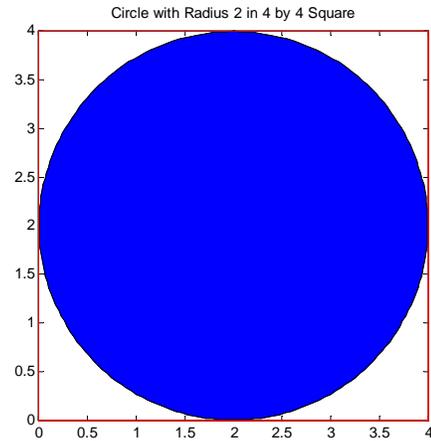


## Lecture 37: Using Monte Carlo Simulations to Find Area of a Circle

### The Idea Behind the Problem

- Place a circle with radius  $r$  in a square that has one corner at the origin.
- Now conduct  $n$  trials where:
  - $x=2*r*rand(1);$
  - $y=2*r*rand(1);$
  - Why don't we use *ceil* in these commands
- if  $(x-r)^2 + (y-r)^2 \leq r^2$  then the point is inside the circle.
- count the number of points  $m$  that fall inside the circle.
- divide it by the number of trials  $n$ .
- thus area of circle will be approximately  $m/n$  times the area of the square  $(2r)^2$ .
- The larger the number of trials, the better the approximations.
- How does this compare to the actual area  $\pi r^2$ ?



### Some Code

```
clf;close all;
success=0;
axis([0,2*r,0,2*r]);
hold on;
for i=1:n;
    x=2*r*rand(1); %find a random x between 0 and 2r
    y=2*r*rand(1); %find a random y between 0 and 2r
    if (x-r)^2+(y-r)^2<=r^2 % success if point is inside or on the circle.
        success=success+1;
        plot(x,y,'r.','MarkerSize',3); %plot red dots on/inside the circle.
    else
        plot(x,y,'b.','MarkerSize',3); %plot blue dots outside the circle.
    end
    if floor(i/1000)==i/1000, disp(i), end;
end
axis square;
area=(success/n)*(2*r)^2; %estimate the area.
a=pi*r^2; %actual area.
title(['Monte Carlo Simulation to find Area of Circle with r=',num2str(r)])
xlabel([num2str(n), ' Trials Conducted. Estimated Area=',num2str(area),' Actual Area=',num2str(a)]);
```

### Homework 37

Adapt the code above to determine the volume of a sphere with radius  $r$ . You will need the *plot3* command and a  $z$  variable to this. Use 10,000 trials to estimate the volume of a sphere with radius 1.33. Compare this to the actual volume. Plot the sphere (note: do not plot the points outside the sphere). A sample output appears below.

$r=0.456$ , Est Vol= $0.40082$ , Act Vol= $0.39718$  (10000 Trials)

